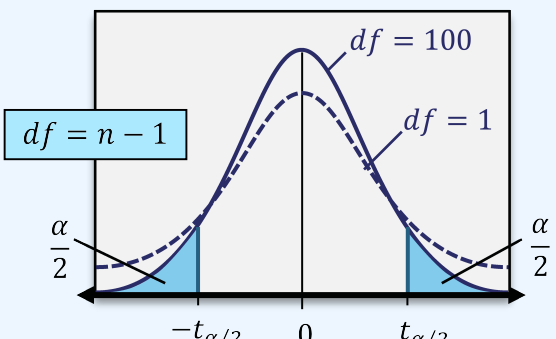
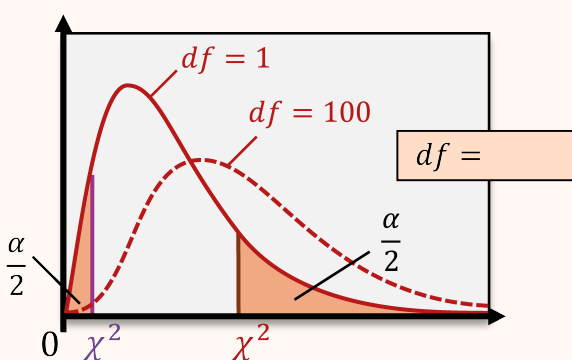


## TOPIC: CONFIDENCE INTERVALS FOR VARIANCE

### Critical Values: Chi Square Distribution

◆ Like the normal &  $t$ -dist., the  $\chi^2$ -dist. is used for confidence intervals but is \_\_\_\_\_ & ALWAYS positive.

Recall	t - Distribution	New	$\chi^2$ - Distribution																																																																							
	 <p><math>t</math>-table: Look up [ 1   2 ] value(s)</p> <p><math>t_{\alpha/2}</math> using <math>\alpha/2</math>, then flip sign for other val.</p> <table border="1" style="margin: 10px auto; border-collapse: collapse;"> <thead> <tr> <th>Conf. Lev.</th> <th>50%</th> <th>...</th> <th>90%</th> <th>95%</th> <th>99%</th> </tr> </thead> <tbody> <tr> <td><math>\downarrow df \mid \alpha/2 \rightarrow</math></td> <td>0.50</td> <td>...</td> <td>0.05</td> <td>0.025</td> <td>0.005</td> </tr> <tr> <td>1</td> <td>1.000</td> <td>...</td> <td>6.314</td> <td>12.71</td> <td>63.66</td> </tr> <tr> <td>2</td> <td>0.816</td> <td>...</td> <td>2.920</td> <td>4.303</td> <td>9.925</td> </tr> <tr> <td>...</td> <td>...</td> <td>...</td> <td>...</td> <td>...</td> <td>...</td> </tr> <tr> <td>30</td> <td>0.683</td> <td>...</td> <td>1.697</td> <td>2.042</td> <td>2.750</td> </tr> </tbody> </table>	Conf. Lev.	50%	...	90%	95%	99%	$\downarrow df \mid \alpha/2 \rightarrow$	0.50	...	0.05	0.025	0.005	1	1.000	...	6.314	12.71	63.66	2	0.816	...	2.920	4.303	9.925	...	...	...	...	...	...	30	0.683	...	1.697	2.042	2.750	 <p><math>\chi^2</math>-table: Look up [ 1   2 ] value(s)</p> <p><math>\chi^2_L</math> using _____ <math>\chi^2_R</math> using _____</p> <table border="1" style="margin: 10px auto; border-collapse: collapse;"> <thead> <tr> <th></th> <th colspan="5">Area to <i>RIGHT</i> of <math>\chi^2</math> Value</th> </tr> <tr> <th><math>df \downarrow</math></th> <th>0.995</th> <th>0.975</th> <th>...</th> <th>0.025</th> <th>0.005</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>--</td> <td>0.001</td> <td>...</td> <td>5.024</td> <td>7.879</td> </tr> <tr> <td>2</td> <td>0.010</td> <td>0.020</td> <td>...</td> <td>7.380</td> <td>10.60</td> </tr> <tr> <td>...</td> <td>...</td> <td>...</td> <td>...</td> <td>...</td> <td>...</td> </tr> <tr> <td>30</td> <td>13.78</td> <td>16.79</td> <td>...</td> <td>46.98</td> <td>53.67</td> </tr> </tbody> </table>		Area to <i>RIGHT</i> of $\chi^2$ Value					$df \downarrow$	0.995	0.975	...	0.025	0.005	1	--	0.001	...	5.024	7.879	2	0.010	0.020	...	7.380	10.60	...	...	...	...	...	...	30	13.78	16.79	...	46.98	53.67
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### EXAMPLE

Find the  $\chi^2$  values for a 95% confidence interval with sample size  $n = 31$ .

$$\begin{array}{ll}
 \alpha = \underline{\hspace{2cm}} & df = \underline{\hspace{2cm}} \\
 \alpha/2 = \underline{\hspace{2cm}} & \chi^2_R = \underline{\hspace{2cm}} \\
 1 - \alpha/2 = \underline{\hspace{2cm}} & \chi^2_L = \underline{\hspace{2cm}}
 \end{array}$$

## TOPIC: CONFIDENCE INTERVALS FOR VARIANCE

### PRACTICE

Use a table to find or estimate  $\chi^2$  such that:

(A)

$$P(X^2 > \chi^2) = 0.010 \text{ (Area to the *right*)}$$

$$df = 50$$

(B)

$$P(X^2 < \chi^2) = 0.010 \text{ (Area to the *left*)}$$

$$df = 50$$

### EXAMPLE

Use a table to find or estimate  $\chi^2$  such that:

$$P(X^2 > \chi^2) = 0.025 \text{ (Area to the *right*)}$$

$$df = 45$$

### PRACTICE

Find the left and right  $\chi^2$ -values for a 99% confidence interval with a sample size of 25.

$$\alpha = \underline{\hspace{2cm}} \quad df = \underline{\hspace{2cm}}$$

$$\alpha/2 = \underline{\hspace{2cm}} \quad \chi^2_R = \underline{\hspace{2cm}}$$

$$1 - \alpha/2 = \underline{\hspace{2cm}} \quad \chi^2_L = \underline{\hspace{2cm}}$$

## **TOPIC: CONFIDENCE INTERVALS FOR VARIANCE**

### **EXAMPLE**

Find the left and right  $\chi^2$ -values for each of the following confidence intervals.

(A) Confidence level = 90%, sample size = 17

$$\alpha = \underline{\hspace{2cm}} \quad df = \underline{\hspace{2cm}}$$

$$\alpha/2 = \underline{\hspace{2cm}} \quad \chi_R^2 = \underline{\hspace{2cm}}$$

$$1 - \alpha/2 = \underline{\hspace{2cm}} \quad \chi_L^2 = \underline{\hspace{2cm}}$$

---

(B) Confidence level = 90%, sample size = 61; Are these values ***closer*** or ***further apart*** than those from (A)?

$$\alpha = \underline{\hspace{2cm}} \quad df = \underline{\hspace{2cm}}$$

$$\alpha/2 = \underline{\hspace{2cm}} \quad \chi_R^2 = \underline{\hspace{2cm}}$$

$$1 - \alpha/2 = \underline{\hspace{2cm}} \quad \chi_L^2 = \underline{\hspace{2cm}}$$

Increasing sample size makes  $\chi^2$ -values

**[ CLOSER | FURTHER APART ]**

---

(C) Confidence level = 99%, sample size = 17; Are these values ***closer*** or ***further apart*** than those from (A)?

$$\alpha = \underline{\hspace{2cm}} \quad df = \underline{\hspace{2cm}}$$

$$\alpha/2 = \underline{\hspace{2cm}} \quad \chi_R^2 = \underline{\hspace{2cm}}$$

$$1 - \alpha/2 = \underline{\hspace{2cm}} \quad \chi_L^2 = \underline{\hspace{2cm}}$$

Increasing sample size makes  $\chi^2$ -values

**[ CLOSER | FURTHER APART ]**