

TOPIC: HYPOTHESIS TESTING USING CRITICAL VALUES

Hypothesis Test: Critical Values & the Rejection Region

◆ A **critical value** (found from α) is the _____ between an "expected" test statistic & an "unusual" one.

P-value

z or $t \rightarrow$ find P -val \rightarrow compare to α

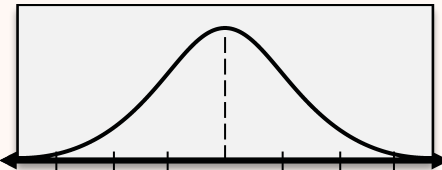
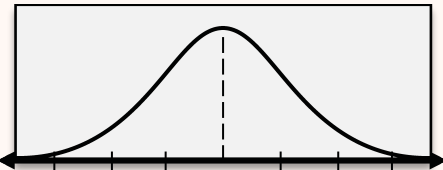
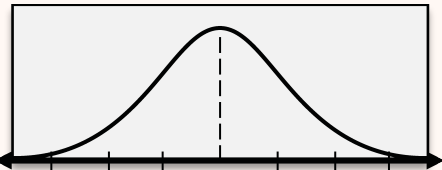
Critical Value

$\alpha \rightarrow$ find Critical Value \rightarrow compare to z or t

► If the test statistic lies in the **rejection region** (area _____ critical value), then we *reject* H_0 .

EXAMPLE

You're a researcher looking at how the current mean age of students in your university has changed from last year, when the mean age was 23. So, you get a sample of students & calculate a test statistic. In each of the following situations, use $\alpha = 0.05$ to find the critical value & determine if the given test stat (z) is in the rejection region.

New Hypothesis Test		
Left Tail	Two Tail	Right Tail
<p>"Students now are younger..."</p> <p>$H_0: \mu = 23; H_a: \mu < 23$</p>  <p>−3 −2 −1 0 1 2 3</p> <p>Critical Val(s): $z_\alpha =$</p> <p>Test Stat: $z = -2.00$</p> <p>z [IN NOT IN] Rejection Region [REJECT FTR] H_0</p>	<p>"Students now have a different mean age..."</p> <p>$H_0: \mu = 23; H_a: \mu \neq 23$</p>  <p>−3 −2 −1 0 1 2 3</p> <p>Critical Val(s): $-z_{\alpha/2} =$ $z_{\alpha/2} =$</p> <p>Test Stat: $z = -1.00$</p> <p>z [IN NOT IN] Rejection Region [REJECT FTR] H_0</p>	<p>"Students now are older..."</p> <p>$H_0: \mu = 23; H_a: \mu > 23$</p>  <p>−3 −2 −1 0 1 2 3</p> <p>Critical Val(s): $z_\alpha =$</p> <p>Test Stat: $z = 0.8$</p> <p>z [IN NOT IN] Rejection Region [REJECT FTR] H_0</p>

TOPIC: HYPOTHESIS TESTING USING CRITICAL VALUES

PRACTICE

Mark 'TRUE' or 'FALSE' for each of the following.

(A) The test statistic & the critical value are the same thing.

[TRUE | FALSE]

(B) The critical value is the boundary of the rejection region.

[TRUE | FALSE]

(C) You should always reject H_0 if the test statistic is greater than the critical value.

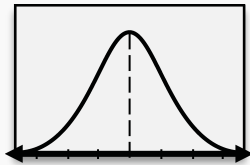
[TRUE | FALSE]

PRACTICE

Use α to find the critical value(s), then determine if the given test statistic is in the rejection region.

(A)

$$H_0: \mu = 7.5; \quad H_a: \mu > 7.5$$
$$\alpha = 0.01; \quad z = 2.17$$



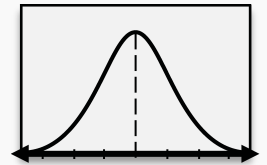
Test is [LEFT | TWO | RIGHT] -tailed

Critical Value(s):

Test stat [IN | NOT IN] rejection region.

(B)

$$H_0: p = 0.64; \quad H_a: p < 0.64$$
$$\alpha = 0.10; \quad z = -1.53$$



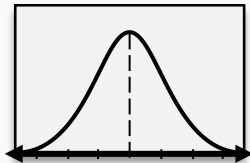
Test is [LEFT | TWO | RIGHT] -tailed

Critical Value(s):

Test stat [IN | NOT IN] rejection region.

(C)

$$H_0: \mu = 98.6; \quad H_a: \mu \neq 98.6$$
$$\alpha = 0.05$$
$$t = 2.41; \quad df = 17$$



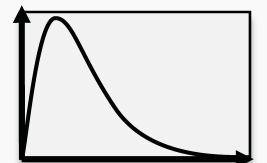
Test is [LEFT | TWO | RIGHT] -tailed

Critical Value(s):

Test stat [IN | NOT IN] rejection region.

(D)

$$H_0: \sigma^2 = 0.3; \quad H_a: \sigma^2 > 0.3$$
$$\alpha = 0.05$$
$$\chi^2 = 61.7; \quad df = 51$$



Test is [LEFT | TWO | RIGHT] -tailed

Critical Value(s):

Test stat [IN | NOT IN] rejection region.

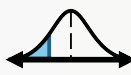
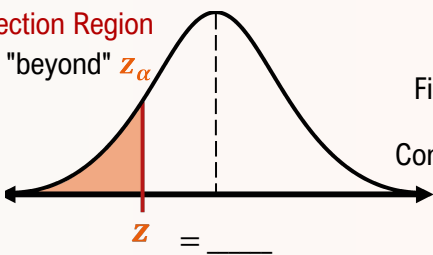
TOPIC: HYPOTHESIS TESTING USING CRITICAL VALUES

Hypothesis Test for Mean Using the Critical Value

◆ The **critical value method** for hyp. tests uses all the same steps as the *P*-value method, except step _____.

EXAMPLE

A soda company claims its cans contain 355 mL on average, but a sample of 50 cans has a mean of 352 mL. Test whether the mean volume is less than claimed using $\alpha = 0.01$ & $\sigma = 5$ mL.

Recall	P-Value Method	New	Critical Value Method
1) Hyp	$H_0: \mu = \underline{\hspace{2cm}}$ $H_a: \mu \underline{\hspace{2cm}}$		
2) Test Stat	$z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$ $\bar{x} = \underline{\hspace{2cm}}$ $\sigma = \underline{\hspace{2cm}}$ $n = \underline{\hspace{2cm}}$ $z = \underline{\hspace{2cm}}$		
3) P-Value	<div style="display: flex; justify-content: space-between;"> <div style="width: 30%;"> <p>Test Stat ↓ Find P-value from test stat ↓ Compare P-val to α</p>  <p>Area "beyond" z $P\text{-value} = \underline{\hspace{2cm}}$</p> </div> <div style="width: 35%; text-align: center;"> <p>3) Critical Value</p>  </div> <div style="width: 30%;"> <p>Test Stat ↓ Find Critical Value from α ↓ Compare Test stat to Crit Val</p> </div> </div>		
4) Conclusion	<p>Because $P\text{-value}$ [< >] α,</p> <p>We [REJECT FAIL TO REJECT] H_0. There is [ENOUGH NOT ENOUGH] evidence that $\mu < 355$.</p>		
Criteria	X is Normally Distributed? <input type="checkbox"/> OR $n > 30$? <input type="checkbox"/>		

TOPIC: HYPOTHESIS TESTING USING CRITICAL VALUES

PRACTICE

A coffee shop owner believes the shop's average daily sales are \$1,200, with a known population standard deviation of \$50. A manager claims it's higher because of their new initiatives & collects a sample of 25 days and finds an average daily sales of \$1,230.

(A) Use $\alpha = 0.10$ & the critical value method to test if the true mean daily sales are higher than \$1200.

Recall

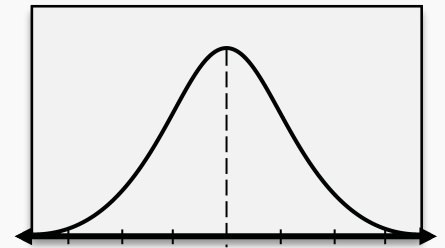
$$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$$

$$H_0: \mu = \underline{\hspace{1cm}} \quad H_a: \mu = \underline{\hspace{1cm}} \quad \bar{x} = \underline{\hspace{1cm}} \quad \sigma = \underline{\hspace{1cm}} \quad n = \underline{\hspace{1cm}}$$

$$z = \underline{\hspace{1cm}}$$

Critical Value(s):

Because test stat. (z) is [**INSIDE** | **OUTSIDE**] rejection region,
we [**REJECT** | **FAIL TO REJECT**] H_0 . There is [**ENOUGH** | **NOT ENOUGH**]
evidence to conclude that...



(B) The owner's policy is to reward store managers with a yearly bonus for increased sales. Should the owner give this manager with the bonus?

EXAMPLE

A company claims that 60% of its customers prefer its new product packaging. A market researcher surveys 200 customers and finds 130 prefer the new packaging. Use $\alpha = 0.05$ & the critical value method test if the true proportion is different from 60%.

$$H_0: p = \underline{\hspace{1cm}} \quad H_a: p = \underline{\hspace{1cm}}$$

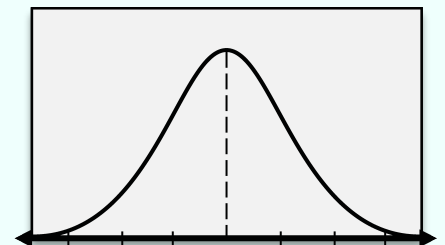
$$x = \underline{\hspace{1cm}} \quad n = \underline{\hspace{1cm}} \quad \hat{p} = \underline{\hspace{1cm}}$$

$$z = \underline{\hspace{1cm}}$$

Critical Value(s):

Recall

$$z = \frac{\hat{p} - p}{\sqrt{p(1-p)/n}}$$



Because test stat. (z) is [**INSIDE** | **OUTSIDE**] rejection region, we [**REJECT** | **FAIL TO REJECT**] H_0 .
There is [**ENOUGH** | **NOT ENOUGH**] evidence to conclude that...